

9. $a = 1 + 3\sqrt{t} \frac{\text{mph}}{\text{sec}}$ for 9 sec

b) How far $\int_0^9 v dt = \text{displacement}$

we need v  also distance if $v > 0$ on $[a, b]$

$$v = \int 1 + 3t^{1/2} dt = t + 3 \frac{t^{3/2}}{3/2} + C \quad t=0$$

$$\text{distance} = \int_0^9 t + 2t^{3/2} dt = 234.9 \text{ mph} \cdot \text{sec} \quad V=0$$

$$234.9 \frac{\text{mi}}{\text{hr}} \cdot \text{sec} \frac{\text{hr}}{3600 \text{ sec}} = .06525 \text{ mi}$$

$$\frac{.06525 \text{ mi} \cdot 5280 \text{ ft}}{\text{mi}}$$

$$344.5 \text{ ft}$$

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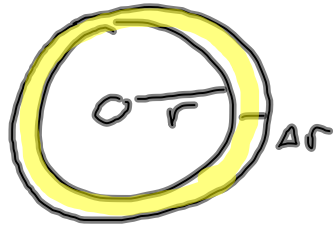
37 $\frac{1}{2} (.04 + 2(.04) + 2(.05) \dots + .05) = .585$

$$\frac{1}{12-0} \int_0^{12} \text{rate } dt$$

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23.

$$\text{density} = 10,000 (2-r) \frac{\text{people}}{\text{mi}^2}$$



area of ring

$$\Delta A \approx 2\pi r \Delta r$$

people in strip $\rightarrow \Delta P \approx$

$$10,000 (2-r) \underbrace{2\pi r \Delta r}_{\text{area}}$$

$$\begin{aligned} \text{Total pop} &\approx \lim_{\Delta r \rightarrow 0} \sum_{i=1}^n 10,000 (2-r_i) 2\pi r_i \Delta r \\ &= \int_0^2 10,000 (2-r) 2\pi r \, dr \\ 83,776 &= \end{aligned}$$

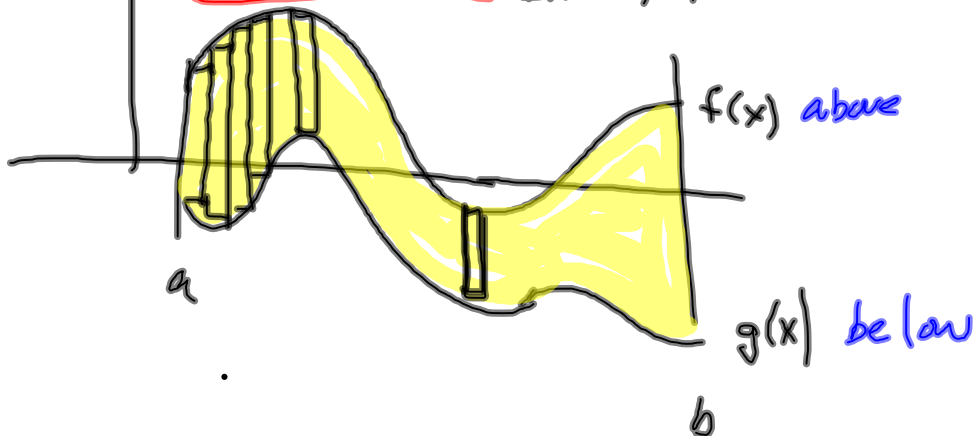
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7.2 area between 2 curves

$$\int_a^b f(x) - g(x) \, dx$$

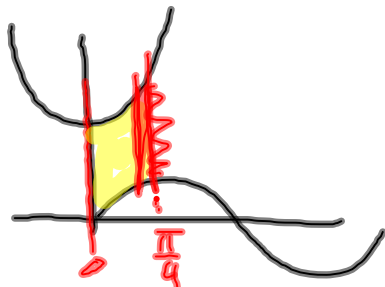
$$\lim_{\Delta x \rightarrow 0} \sum_{i=1}^n [f(x_i) - g(x_i)] \Delta x$$

height · width



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Find the area between $y = \sec^2 x$ & $y = \sin x$
on $[0, \frac{\pi}{4}]$



$$\int_0^{\pi/4} \sec^2 x - \sin x \, dx$$

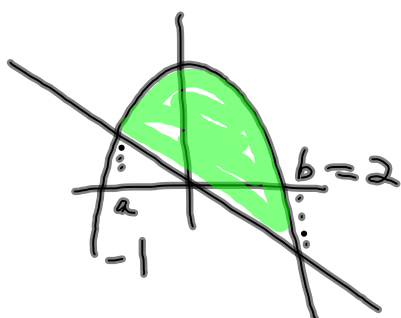
$$\tan x + \cos x \Big|_0^{\pi/4}$$

$$\tan \frac{\pi}{4} + \cos \frac{\pi}{4} - (\tan 0 + \cos 0)$$

$$1 + \frac{\sqrt{2}}{2} - 1 = \frac{\sqrt{2}}{2}$$

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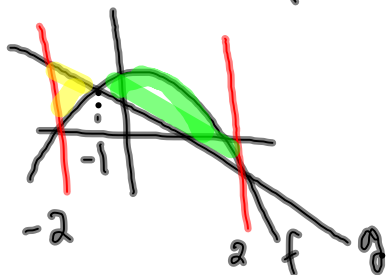
Find the area bound by $y = 2 - x^2$ & $y = -x$



$$2 - x^2 = -x$$

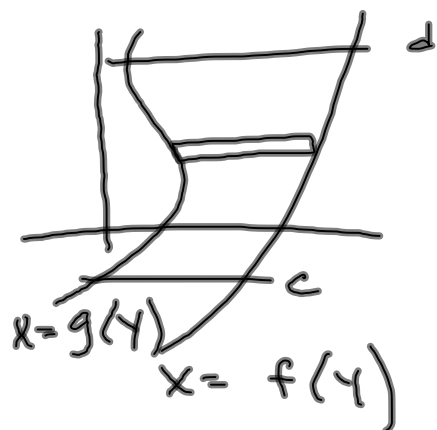
$$0 = x^2 - x - 2 = (x - 2)(x + 1)$$

$$\int_{-1}^2 (2 - x^2 - (-x)) \, dx = \frac{9}{2}$$



$$\int_{-2}^{-1} g - f \, dx + \int_{-1}^2 f - g \, dx$$

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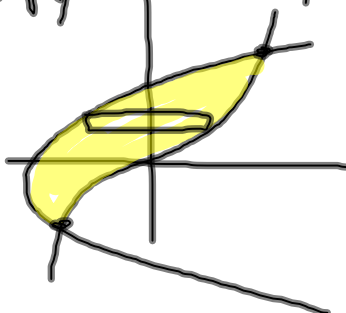
$$\text{Area} = \int_c^d \overset{\text{right}}{f(y)} - \overset{\text{left}}{g(y)} dy$$

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Ex 6

$$y = x^3 \quad x = y^{1/3}$$

$$x = \sqrt[3]{y} \rightarrow x = y^{1/3}$$



$$x = y^2 - 2$$

$$\int_{-1}^{1.7930} y^{1/3} - (y^2 - 2) dy$$

$$\underline{y^{1/3} = y^2 - 2} \quad \text{use to find } c, d$$

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